Pairing and Superfluidity in Atomic Fermi Mixtures

Henk Stoof

- (Very Long) Introduction
- BCS Theory
- The BEC-BCS Crossover and Imbalanced Fermi Mixtures
- Renormalization Group Theory





Ideal Fermi Gases I

• Experiments are always in a trap:



Ideal Fermi Gases II

• Number of states below a certain energy (for one spin state) is:

$$N(\varepsilon) = \frac{1}{(\hbar\omega)^3} \int_0^{\varepsilon} d\varepsilon_x \int_0^{\varepsilon - \varepsilon_x} d\varepsilon_y \int_0^{\varepsilon - \varepsilon_x - \varepsilon_y} d\varepsilon_z = \frac{\varepsilon^3}{6(\hbar\omega)^3}$$

• This means that the Fermi energy is:

$$\varepsilon_F = (6N)^{1/3} \hbar \omega$$

Ideal Fermi Gases III

• Differently: For the homogeneous gas: $n = k_F^3 / 6\pi^2$. So in the trap

$$n(\mathbf{x}) = \frac{1}{6\pi^2} \left\{ \frac{2m}{\hbar^2} [\varepsilon_F - V(\mathbf{x})] \right\}^{3/2}$$

• By integrating over space we find again:

$$\varepsilon_F = (6N)^{1/3} \hbar \omega$$

• Note that the size of the cloud is: R

$$=\sqrt{\frac{2\varepsilon_F}{m\omega^2}}$$

Ideal Fermi Gases IV

• Comparison between bosons and fermions:



Ultracold Fermi Mixtures I

Experimental control over:



- temperature and density
- external potentials, disorder
- number of particles, their

quantum state

and even interactions!



- Degenerate Fermi mixtures
 - Neutron stars
 - (High-Tc) superconductors

 $(T = 10^{6} \text{ K}, T_{F} = 10^{11} \text{ K}, T = 10^{-5} T_{F})$ $(T = 10^2 \text{ K}, T_F = 10^5 \text{ K}, T = 10^{-3} T_F)$ - Ultracold atomic Fermi gases $(T = 10^2 \text{ nK}, T_F = \mu \text{K}, T = 10^{-1} T_F)$

Ultracold Fermi Mixtures II

• Collisions are *s*-wave

$$\hbar k_F r_V \ll \hbar$$

and we thus only have interactions between two different spin states.



• This implies also:

$$nr_V^3 \ll 1$$

Ultracold Fermi Mixtures III

• Hyperfine and Zeeman interactions:



- Central or exchange interaction
- Together they lead to Feshbach resonances!



Ultracold Fermi Mixtures IV



Superfluidity I

• Flow without friction. Described by a macroscopic wave function: $i(m\mathbf{x}/\hbar)\cdot\mathbf{x}$

$$\Psi(\mathbf{x}) = \sqrt{n_s} e^{i(m\mathbf{v}_s/\hbar) \cdot \mathbf{x}}$$

or more general $\mathbf{v}_s(\mathbf{x}) = \hbar \nabla \mathcal{G}(\mathbf{x}) / m$ and $n_s(\mathbf{x}) = |\Psi(\mathbf{x})|^2$.

• This implies the existence of quantized vortices with

$$\mathcal{G}(\mathbf{x}) = \ell \varphi$$

which is really the trademark of superfluidity.



Superfluidity II

• Observed in a rotating Bose-Einstein condensate:



• What about a Fermi gas?





BCS

BEC

Superfluidity III

• Presently much debate over:





$$P = 0$$

P = 1

BEC I

• In second-quantization language the hamiltonian is

$$\widehat{H} = \int d\mathbf{x} \,\widehat{\psi}^{\dagger}(\mathbf{x}) \left\{ -\frac{\hbar^2 \nabla^2}{2m} - \mu \right\} \widehat{\psi}(\mathbf{x}) + \dots$$
$$\dots + \frac{1}{2} V_0 \int d\mathbf{x} \,\widehat{\psi}^{\dagger}(\mathbf{x}) \widehat{\psi}^{\dagger}(\mathbf{x}) \widehat{\psi}(\mathbf{x}) \widehat{\psi}(\mathbf{x}),$$

• How do we treat Bose-Einstein condensation now?

BEC II

• Our most simple variational ground-state wave function for a Bose-Einstein condensed gas is now

$$|\Psi\rangle \propto \left(\int d\mathbf{x}\,\phi(\mathbf{x})\widehat{\psi}^{\dagger}(\mathbf{x})\right)^{N}|0\rangle.$$

• However, for $N \gg 1$ we expect that we are also allowed to use the more convenient wave function

$$|\Psi\rangle \propto \exp\left(\int d\mathbf{x}\,\phi(\mathbf{x})\widehat{\psi}^{\dagger}(\mathbf{x})\right)|0\rangle$$
.

BEC III

• The latter ground-state wave function has the property that

$$\hat{\psi}(\mathbf{x}) |\Psi\rangle = \phi(\mathbf{x}) |\Psi\rangle.$$

• This suggests that Bose-Einstein condensation is associated with spontaneous symmetry breaking, i.e.,

$$\langle \hat{\psi}(\mathbf{x}) \rangle \neq 0.$$

• This is the macroscopic wavefunction of superfluidity!

Symmetry Breaking I

• It is nice to understand spontaneous symmetry breaking a bit better. At a fixed number we have

$$|N\rangle \propto \frac{1}{\sqrt{N!}} \left(\int dx \, \phi(x) \widehat{\psi}^{\dagger}(x) \right)^{N} |0\rangle.$$

• At fixed phase we have, however,

$$|\vartheta\rangle \propto \sum_{N} \frac{\exp(iN\vartheta)}{\sqrt{N!}} |N\rangle.$$

Symmetry Breaking II

• This shows that the phase and the number of particles are conjugate variables, i.e.,

$$[N,\mathcal{G}]_{-}=-i.$$

• Moreover, the energy obeys due to the definition of the chemical potential

$$E \simeq E_0 + \mu \Delta N + \frac{1}{2} \frac{d \mu}{dN} \Delta N^2.$$

Symmetry Breaking III

• The thermodynamic potential thus obeys

$$\Omega \simeq \Omega_0 + \frac{1}{2} \frac{d\mu}{dN} \Delta N^2,$$

• which leads to the Schrödinger equation

$$i\hbar\frac{\partial}{\partial t}\Psi(\vartheta) = \frac{1}{2}\frac{d\mu}{dN}\left(\frac{1}{i}\frac{\partial}{\partial\vartheta} - N\right)^2\Psi(\vartheta).$$

Symmetry Breaking IV

• So the absolute ground state of the gas is the symmetry unbroken state

$$\Psi(\vartheta) = \frac{1}{\sqrt{2\pi}} \exp(iN\vartheta).$$

• However, if $N \gg 1$ it takes a very long time for the gas to 'diffuse' to this state and we can safely assume that

$$\Psi(\mathcal{G}) = \delta(\mathcal{G}).$$

BCS I

• In second-quantization language the hamiltonian is

$$\widehat{H} = \sum_{\sigma} \int d\mathbf{x} \,\widehat{\psi}_{\sigma}^{\dagger}(\mathbf{x}) \left\{ -\frac{\hbar^2 \nabla^2}{2m} - \mu_{\sigma} \right\} \widehat{\psi}_{\sigma}(\mathbf{x}) + \dots$$
$$\dots + V_0 \int d\mathbf{x} \,\widehat{\psi}_{\uparrow}^{\dagger}(\mathbf{x}) \widehat{\psi}_{\downarrow}^{\dagger}(\mathbf{x}) \widehat{\psi}_{\downarrow}(\mathbf{x}) \widehat{\psi}_{\uparrow}(\mathbf{x}),$$

• Now we have Bose-Einstein condensation of pairs so:

$$\left\langle \widehat{\psi}_{\downarrow}(\mathbf{x})\widehat{\psi}_{\uparrow}(\mathbf{x})\right\rangle \neq 0.$$

BCS II

• Introducing $\Delta = V_0 \left\langle \widehat{\psi}_{\downarrow}(\mathbf{x}) \widehat{\psi}_{\uparrow}(\mathbf{x}) \right\rangle$ the Hamiltonian can be approximated by

$$\widehat{H} \simeq \sum_{\sigma} \int d\mathbf{x} \,\widehat{\psi}_{\sigma}^{\dagger}(\mathbf{x}) \left\{ -\frac{\hbar^2 \nabla^2}{2m} - \mu_{\sigma} \right\} \widehat{\psi}_{\sigma}(\mathbf{x}) + \dots \\ \dots + \int d\mathbf{x} \,\Delta \widehat{\psi}_{\uparrow}^{\dagger}(\mathbf{x}) \widehat{\psi}_{\downarrow}^{\dagger}(\mathbf{x}) + \int d\mathbf{x} \Delta^* \widehat{\psi}_{\downarrow}(\mathbf{x}) \widehat{\psi}_{\uparrow}(\mathbf{x}),$$

• This is thus a mean-field theory!

Zero Temperature I

- The microscopic Hamiltonian

$$\hat{H} = \sum_{\mathbf{k},\alpha} (\epsilon_{\mathbf{k}} - \mu_{\alpha}) \hat{\psi}^{\dagger}_{\mathbf{k},\alpha} \hat{\psi}_{\mathbf{k},\alpha} + \frac{V_0(\Lambda)}{V} \sum_{\mathbf{K},\mathbf{k},\mathbf{k}'} \hat{\psi}^{\dagger}_{\mathbf{K}-\mathbf{k}',\uparrow} \hat{\psi}^{\dagger}_{\mathbf{k}',\downarrow} \hat{\psi}_{\mathbf{K}-\mathbf{k},\downarrow} \hat{\psi}_{\mathbf{k},\uparrow}$$

- Interaction vs. scattering length

$$V_0(\Lambda) = \frac{4\pi\hbar^2 a}{m} \frac{\pi}{\pi - 2a\Lambda}$$

- The BCS Ansatz

$$\Psi_{\rm BCS}\rangle = \prod_{\mathbf{k}} \left(u_{\mathbf{k}} + v_{\mathbf{k}} \hat{\psi}^{\dagger}_{-\mathbf{k},\uparrow} \hat{\psi}^{\dagger}_{\mathbf{k},\downarrow} \right) |0\rangle$$

- Expectation values

$$\langle \Psi_{\rm BCS} | \hat{\psi}^{\dagger}_{\mathbf{k},\alpha} \hat{\psi}_{\mathbf{k},\alpha} | \Psi_{\rm BCS} \rangle = v_{\mathbf{k}}^{2}, \\ \langle \Psi_{\rm BCS} | \hat{\psi}_{\mathbf{k},\downarrow} \hat{\psi}_{-\mathbf{k},\uparrow} | \Psi_{\rm BCS} \rangle = u_{\mathbf{k}} v_{\mathbf{k}}$$



Zero Temperature II

- Normalization and minimization of $\langle \Psi_{BCS} | \hat{H} | \Psi_{BCS} \rangle$,

$$v_{\mathbf{k}}^2 = 1 - u_{\mathbf{k}}^2 = \frac{1}{2} \left(1 - \frac{\epsilon_{\mathbf{k}} - \mu}{\hbar \omega_{\mathbf{k}}} \right)$$
 with
 $\hbar \omega_{\mathbf{k}} = \sqrt{(\epsilon_{\mathbf{k}} - \mu)^2 + \Delta^2}$.

- Gap and number equation:

$$\begin{split} \Delta &\equiv -\frac{V_0(\Lambda)}{V}\sum_{\mathbf{k}} u_{\mathbf{k}} v_{\mathbf{k}} \\ n &= \frac{2}{V}\sum_{\mathbf{k}} v_{\mathbf{k}}^2 \quad . \end{split}$$

- We have introduced:

$$\mu = (\mu_\uparrow + \mu_\downarrow)/2 ~~{\rm and}~~ h = (\mu_\uparrow - \mu_\downarrow)/2$$
 .





Summary

• BEC:

$$|\Psi\rangle \propto \exp\left(\int d\mathbf{x}\,\phi(\mathbf{x})\widehat{\psi}^{\dagger}(\mathbf{x})\right)|0\rangle$$
.

• BCS:

$$|\Psi\rangle \propto \exp\left(\int d\mathbf{x} \, d\mathbf{x}' \phi(\mathbf{x}, \mathbf{x}') \widehat{\psi}_{\downarrow}^{\dagger}(\mathbf{x}) \widehat{\psi}_{\uparrow}^{\dagger}(\mathbf{x}')\right) |0\rangle$$

leads to gap equation for $\Delta(\mathbf{x}) = V_0 \langle \widehat{\psi}_{\downarrow}(\mathbf{x}) \widehat{\psi}_{\uparrow}(\mathbf{x}) \rangle$.

The BEC-BCS Crossover I

- Cooper condensate wavefunction:

$$\phi_{\mathbf{0}}(\mathbf{r}) = -\frac{1}{V} \sum_{\mathbf{k}} u_{\mathbf{k}} v_{\mathbf{k}} e^{-i\mathbf{k}\mathbf{r}}$$

- Fermi energy

$$\epsilon_{\rm F} = \hbar^2 k_{\rm F}^2 / 2m = \hbar^2 (3\pi^2 n)^{2/3} / 2m$$







The BEC-BCS Crossover II

MIT: the study of vortices Innsbruck: the study of collective modes





Imbalanced Fermi Gas at Unitarity

- Mean-field substitution, where $V_0 \langle \hat{\psi}_{\downarrow}(\mathbf{x}) \hat{\psi}_{\uparrow}(\mathbf{x}) \rangle \equiv \Delta$, such that

 $V_0 \hat{\psi}^{\dagger}_{\uparrow}(\mathbf{x}) \hat{\psi}^{\dagger}_{\downarrow}(\mathbf{x}) \hat{\psi}_{\downarrow}(\mathbf{x}) \hat{\psi}_{\uparrow}(\mathbf{x}) \rightarrow \Delta^* \hat{\psi}_{\downarrow}(\mathbf{x}) \hat{\psi}_{\uparrow}(\mathbf{x}) + \Delta \hat{\psi}^{\dagger}_{\uparrow}(\mathbf{x}) \hat{\psi}^{\dagger}_{\downarrow}(\mathbf{x}) - \Delta^2 / V_0$

- Mean-field Hamiltonian,

$$\frac{\hat{H}}{V} = \sum_{\mathbf{k}} \frac{\epsilon_{\mathbf{k}} - \mu_{\downarrow}}{V} + \frac{1}{V} \sum_{\mathbf{k}} \begin{bmatrix} \hat{\psi}^{\dagger}_{\mathbf{k},\uparrow}, \hat{\psi}_{-\mathbf{k},\downarrow} \end{bmatrix} \begin{bmatrix} \epsilon_{\mathbf{k}} - \mu_{\uparrow} & \Delta \\ \Delta^{*} & \mu_{\downarrow} - \epsilon_{\mathbf{k}} \end{bmatrix} \begin{bmatrix} \hat{\psi}_{\mathbf{k},\uparrow} \\ \hat{\psi}^{\dagger}_{-\mathbf{k},\downarrow} \end{bmatrix} - \frac{|\Delta|^2}{V_0}$$

- The Bogoliubov quasi-particles, $\hat{\phi}_{\mathbf{k},\uparrow} = u_{\mathbf{k}}\hat{\psi}_{\mathbf{k},\uparrow} - v_{\mathbf{k}}\hat{\psi}^{\dagger}_{-\mathbf{k},\downarrow}$ $\hat{\phi}^{\dagger}_{-\mathbf{k},\downarrow} = v_{\mathbf{k}}\hat{\psi}_{\mathbf{k},\uparrow} + u_{\mathbf{k}}\hat{\psi}^{\dagger}_{-\mathbf{k},\downarrow}$
- The quasi-particle dispersions, $\hbar\omega_{{\bf k},\uparrow/\downarrow} = \mp h + \sqrt{(\epsilon_{{\bf k}} - \mu)^2 + \Delta^2}$



Sarma Phase

- BCS ground state energy and ideal gas of quasi-particles

 $\frac{\hat{H}}{V} = -\frac{\Delta^2}{V_0(\Lambda)} + \frac{1}{V} \sum_{\mathbf{k},\alpha} \left\{ -\hbar\omega_{\mathbf{k},\alpha} v_{\mathbf{k}}^2 + \hbar\omega_{\mathbf{k},\alpha} \hat{\phi}_{\mathbf{k},\alpha}^{\dagger} \hat{\phi}_{\mathbf{k},\alpha} \right\}$

- In principle, majority becomes gapless, when $\Delta = h$.
- Then, ground state becomes gapless polarized superfluid.
- Occupation numbers:

$$\langle \hat{\psi}^{\dagger}_{\mathbf{k},\alpha} \hat{\psi}_{\mathbf{k},\alpha} \rangle \equiv n_{\mathbf{k},\alpha}.$$

-Typically, Sarma phase is unstable at zero temperature.



Thermodynamics

- Thermodynamic potential density

$$\omega_{\rm BCS} = -\frac{\Delta^2}{V_0(\Lambda)} + \frac{1}{V} \sum_{\mathbf{k}} \left\{ \hbar \omega_{\mathbf{k}} - \epsilon_{\mathbf{k}} + \mu \right\} - \frac{1}{\beta V} \sum_{\mathbf{k},\alpha} \log \left(1 + e^{-\beta \hbar \omega_{\mathbf{k},\alpha}} \right).$$



Homogeneous Phase Diagram



The Local-Density Approximation (LDA)

-Trapping potential: $V_{\text{trap}}(\mathbf{r}) = \frac{1}{2}m\omega_{\text{trap}}^2r^2$

- LDA : $\mu_{\alpha}(\mathbf{r}) \equiv \mu_{\alpha} V_{\text{trap}}(\mathbf{r})$
- In the trap: decreasing $\mu(\mathbf{r})$, constant *h*.





Phase Diagram in a Trap

- Superfluid phase: 2nd order transition in the trap.
- Phase separation: 1st order transition in the trap.
- Normal phase: normal throughout trap.





(Global) polarization: $P = \frac{N_{\uparrow} - N_{\downarrow}}{N_{\uparrow} + N_{\downarrow}}$

'Old' MIT Experiments





Shell structure with fully paired core and normal outer region.

1st or 2nd order?

'New' MIT Experiment: Homogeneous Phase Diagram

• Measurements locally in the trap. For the first time MIT also experimentally show phase separation.



• Not understood why Rice sees deformation and no upper critical imbalance (known as Clogston limit).

The Rice Experiments

• Typical gas clouds with superfluid core at MIT.



Shin et al., PRL 97, 030401 (2006)

No deformation

• Gas clouds at lowest and higher temperature of Rice



Partridge et al., PRL 97, 190407 (2006)

a) Deformation c) No deformation

Zero T, Unitary, Normal Phase: MC Equation of State

?

• Spin-down particle in sea of spin-up particles: fermion or Cooper pair?



• Dashed line $E(N_{\uparrow}, N_{\downarrow}) = \frac{3}{5} E_{F,\uparrow} N_{\uparrow} + \frac{3}{5} E_{F,\downarrow} N_{\downarrow} - 0.6 E_{F,\uparrow} N_{\downarrow}$

Remember! $\hbar \Sigma_{\downarrow} = -0.6 E_{F,\uparrow}$

• Quantum phase transition at P = 0.39 (homogeneous) and P = 0.78 (trap with LDA)!





Lobo et al., PRL 97, 200403 (2006)

Renormalization Group Approach

- Integrate out modes in high-momentum shell Λ of width $d\Lambda$. Absorb result in couplings. Integrate out new shell, etc.
- Use RG as (non-perturbative) method to solve iteratively many-body problem.
- Starting point. The microscopic action

$$S = \sum_{\mathbf{k},n} \phi_{\sigma,\mathbf{k},n}^* (-i\hbar\omega_n - \varepsilon_{\mathbf{k}} - \mu_{\sigma}) \phi_{\sigma,\mathbf{k},n} + \sum_{\substack{\mathbf{q},\mathbf{k},\mathbf{k}',\\m,n,n'}} \Gamma_{\mathbf{q},m} \phi_{\uparrow,\mathbf{q}-\mathbf{k},m-n}^* \phi_{\downarrow,\mathbf{k},n}^* \phi_{\downarrow,\mathbf{k}',n'} \phi_{\uparrow,\mathbf{q}-\mathbf{k}',m-n'}$$

- Technically, we have to calculate one-loop diagrams.
- Infinitesimal width makes higher-loop diagrams vanish.



RG Theory for Imbalanced Fermi Gas

• Integrate out momenta in a shell Λ of infinitesimal width $d\Lambda$. Renormalization of chemical potentials determines fermionic self-energy.

$$d\mu_{\sigma} = -\frac{\Lambda^2}{2\pi^2} \Gamma_{\mathbf{0},0} N_{-\sigma} d\Lambda$$

Due to infinitesimal width higher loop diagrams vanish!



• Interaction: 'ladder diagram' (scattering of particles), 'bubble diagram' (screening by particle-hole excitations). Coupled diff. equations!

$$d\Gamma_{\mathbf{0},0}^{-1} = \frac{\Lambda^2}{2\pi^2} \left(\frac{1 - N_{\uparrow} - N_{\downarrow}}{2(\varepsilon_{\Lambda} - \mu)} - \frac{N_{\uparrow} - N_{\downarrow}}{2h} \right) d\Lambda \quad , \quad N_{\sigma} = \frac{1}{e^{\beta(\varepsilon_{\Lambda} - \mu_{\sigma})} + 1} \quad , \quad \varepsilon_{\Lambda} = \frac{\hbar^2 \Lambda^2}{2m}$$

• Phase transition: $\Gamma_{0,0}(\infty)$ diverges (Thouless criterion). Self-energies diverge. Unphysical! CM-momentum/frequency dependence important! $\Gamma_{\mathbf{q},m}^{-1} = \Gamma_{0,0}^{-1} - Z_q^{-1}q^2 + Z_{\omega}^{-1}i\hbar\omega_m$

RG Theory for T=0, Unitary, Extremely Imbalanced Gas

• One spin-down particle in a sea of spin up particles. Density of spin-down particles is zero. Self energy due to strong interactions (unitarity limit).

$$d\Gamma_{\mathbf{0},0}^{-1} = \frac{\Lambda^2}{2\pi^2} \left(\frac{1 - N_{\uparrow}}{2(\varepsilon_{\Lambda} - \mu_{\downarrow})} - \frac{N_{\uparrow}}{2h} \right) d\Lambda$$
$$d\mu_{\downarrow} = -\frac{\Lambda^2}{2\pi^2(\Gamma_{\mathbf{0},0}^{-1} - Z_q q^2)} N_{\uparrow} d\Lambda$$

• QPT from zero to nonzero down-density at

$$\begin{split} E_{F,\downarrow} &= \mu_{\downarrow}(\infty) = 0 = \mu_{\downarrow}(0) - \hbar \Sigma_{\downarrow} \\ \hbar \Sigma_{\downarrow} &= -0.6 \mu_{\uparrow} = -0.6 E_{F,\uparrow} \end{split}$$

• Crucial to let chemical potential flow!





RG Theory: Weakly Interacting, Balanced Fermi Gas

• In the extremely weakly interacting limit the chemical potentials don't renormalize anymore, i.e. the selfenergies go to zero

$$d\Gamma_{\mathbf{0},0}^{-1} = \frac{\Lambda^2}{2\pi^2} \left(\frac{1-2N}{2(\varepsilon_{\Lambda} - \mu)} - \beta N(1-N) \right) d\Lambda$$

- Differential form of gap equation with (some kind of) Gorkov's correction $\epsilon_{\Lambda_0 l}$
- Flow to (stationary) Fermi surface. Natural endpoint because here excitations of lowest energy.
 - Exactly solvable! Leads to the BCS transition temperature reduced by a factor of *e* (with relative momentum it is 2.2)



RG Theory: Unitarity Limit, Imbalanced Case

• Three Fermi levels in the system! But only one pole in RG equations

$$d\Gamma_{\mathbf{0},0}^{-1} = \frac{\Lambda^2}{2\pi^2} \left(\frac{1 - N_{\uparrow} - N_{\downarrow}}{2(\varepsilon_{\Lambda} - \mu)} - \frac{N_{\uparrow} - N_{\downarrow}}{2h} \right) d\Lambda$$
$$d\mu_{\sigma} = -\frac{\Lambda^2}{2\pi^2 (\Gamma_{\mathbf{0},0}^{-1} - Z_q q^2)} N_{-\sigma} d\Lambda$$

- Flow automatically to average Fermi level
- Tricritical point determined by following class of Feynman diagram



• Again, flowing of $\mu(l)$ crucial, since $\mu(0)/\mu(\infty) = 1 + \beta$



Conclusion and Outlook I

- Ultracold quantum gases are ideal quantum simulators. The field is able to address fundamental questions on many-body quantum systems in great detail.
- A first good example is the detailed study of the BEC-BCS crossover, which gives a unified view on BEC- and BCS-like superfluidity.
- A second example is the study of the strongly interacting Fermi mixture with a population imbalance, whose phase diagram is important to condensed matter, nuclear matter and astrophysics.
- Many more examples are under way. Fermi mixtures with a mass imbalance, with long-ranged anisotropic dipole interactions, the doped fermionic Hubbard model, etc. We recently worked on:

Conclusion and Outlook II

• Superfluid-normal interface and surface tension:



Conclusion and Outlook III

• Mass imbalance (⁶Li-⁴⁰K) at unitarity:



Conclusion and Outlook IV

• Imbalanced antiferromagnet:



The Quantum Fluids and Solids Group

 Students: Arnoud Koetsier Koos Gubbels Jeroen Diederix Jasper van Heugten Jildou Baarsma

Postdoc's: Vacancy!

■ Staff: Henk Stoof

